Chlorite control of correlations between strain and anisotropy of magnetic susceptibility

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Anisotropy of magnetic susceptibility (AMS) has in the past been used as an indicator of finite strain; mathematical relationships between the measured AMS ellipsoid and the finite strain ellipsoid in slates are numerous. The Ordovician Martinsburg Formation at Lehigh Gap, Pennsylvania, provides a unique opportunity to test this correlation, as a complete shale-to-slate transition is preserved. Magnitudes of the principal susceptibility axes appear to reflect a strain gradient at this location. Apparent strain values derived from AMS, using equations from Rathore and Hrouda, have $X/Y/Z$ ratios from 2.79:1.87:0.19 (shale) to 2.92:0.82:0.42 (slate). The orientations of the susceptibility axes characterize two fabrics: (i) $k_{int}/k_{max}$ planes at 20° to bedding and (ii) $k_{int}/k_{max}$ planes parallel to cleavage. Anisotropy of magnetic susceptibility fails to show any intermediate orientations of the principal susceptibility axes in the zone in which cleavage is developed. Comparison with phyllosilicate crystallographic orientations indicates that the AMS intermediate and maximum susceptibility axes are parallel to chlorite basal planes. Because chlorite reoriented via dissolution and new growth as cleavage developed in this location, and because models correlating AMS and strain instead assume that strain is reflected by the rotation of the magnetic susceptibility carriers, the apparent strain values calculated from AMS reflect only the degree of dissolution and neocrystallization in these rocks and not the finite strain.

1. Introduction

Anisotropy of magnetic susceptibility (AMS) has been widely used in the analysis of rock fabrics and strain. Analysis of AMS determines the combined susceptibility of paramagnetic, diamagnetic and ferrimagnetic minerals to an induction field in a sample. Studies in a variety of rock types have demonstrated that rock fabrics, such as bedding and cleavage, are reflected in the orientation of AMS principal axes (e.g. Kligfield et al., 1977; Borradaile, 1987; Rochette, 1987; Goldstein and Brown, 1988; Hirt et al., 1988; Hrouda et al., 1988). Combined studies of strain and AMS in rocks commonly attempt to correlate values of finite strain with the AMS ellipsoid, which is determined by the magnitudes (lengths) of the principal susceptibility axes. Various mathematical relationships between finite strain and AMS ellipsoids have been proposed (Owens, 1974; Wood et al., 1976; Rathore, 1979, 1988; Hrouda, 1980, 1987; Cogne and Perroud, 1988). Rathore (1979) and Hrouda (1987) related the ratios of principal susceptibility axes to March strains in slates using an exponential function based on the work by Owens (1974) and Wood et al. (1976). In contrast, Cogne and Perroud (1988) reported that the shapes and axial dimensions of the AMS ellipsoid and the strain ellipsoid were similar for a granite pluton. Experimental studies, however, have not demonstrated a direct correlation between strain and AMS; they reveal a consistent change in AMS fabric with increasing strain (Borradaile and Alford, 1987, 1988). In these experi-
ments, the correlation between AMS and rock fabric is imperfect however. The problem in correlating rock fabrics and strain with AMS may arise from differing contributions of diamagnetic (e.g. calcite), paramagnetic (e.g. chlorite) and ferromagnetic (e.g. magnetite) minerals in a single sample. Borradaile (1988) noted that the ability of AMS to indicate rock fabric and strain may be improved when a single mineral determines the AMS.

This study examines the AMS of the Martinsburg Formation at Lehigh Water Gap, Pennsylvania (Fig. 1). The Martinsburg Formation in this location preserves the transition from an uncleaved shale at the contact with the overlying Shawangunk Formation to a well-cleaved slate over an interval of approximately 130 m. The uncleaved shale displays moderate to well-developed bedding, which on average dips 40° NNW. Incipient cleavage is first observed ~75 m from the Shawangunk Formation contact, and cleavage development gradually increases in the interval of 75–120 m from the Shawangunk Formation contact. When fully developed, the slaty cleavage is pervasive and is consistently oriented perpendicular to the bedding plane, with an average dip of 60° SSE.

The shale-to-slate transition at this outcrop has been studied extensively (Anonymous, 1885; McBride, 1962; Drake and Epstein, 1967; Epstein and Epstein, 1969; Holeywell and Tullis, 1975; Wintsch, 1978; Lee et al., 1986). Holeywell and Tullis (1975) and Wintsch (1978) considered this transition to be preserved in a pressure-shadow that was caused by the unconformably overlying Shawangunk Formation. Detailed microstructural study has indicated that dissolution and new growth of phyllosilicates characterizes the formation of cleavage in this outcrop (Lee et al., 1986).

Samples for AMS study were collected from 18 sites along this outcrop. The results of this study illustrate how changes in rock fabric and strain are manifested in magnetic fabrics when chlorite dominates the magnetic anisotropy.

2. Sampling and analysis

Oriented blocks comprising 18 sites were collected at regular intervals in a single, continuous outcrop from the Martinsburg—Shawangunk contact to a distance of 130 m (measured horizontally). Locations and site numbers were selected to
facilitate comparison with the results of X-ray texture goniometry data from Holeywell and Tullis (1975). Intact samples were difficult to extract from the outcrop owing to extensive fracturing. After the orientation was marked, blocks were covered with masking tape to prevent cracking of the sample prior to removal. The oriented blocks were then removed and wrapped completely in tape to prevent further breakage during transport. Once in the lab, the blocks were glued together, then coated with a thick layer of epoxy. Blocks were then mounted on a drill press and cores were drilled with a water-cooled drill. Each site provided three to five cores with a diameter of 2.5 cm and a length of 2.2 cm. The AMS was measured with a Sapphire Instruments SI-2 susceptibility bridge with digital interface connected to a PC. Each analysis provides the orientations and magnitudes, as well as precision estimates, of the minimum, intermediate and maximum susceptibility axes (Stupavsky, 1984).

3. Results

Results of AMS analysis for the Martinsburg Formation display two distinct fabrics (Fig. 2), (i) a 'no-cleavage' fabric in which the minimum axis is generally $20^\circ$ steeper than the bedding pole, and (ii) a 'cleavage' fabric in which the minimum axis is at a high angle to the cleavage plane. For many of the cleaved samples the maximum axis is at the bedding–cleavage intersection. The AMS fabric, as seen in the orientation of the three AMS ellipsoid axes, changes abruptly from the 'no-cleavage' fabric to the 'cleavage' fabric at a point ~ 75 m from the Shawangunk Formation contact. This abrupt change in AMS orientation is in marked contrast to the gradual development of cleavage reported over this interval (e.g. Holeywell and Tullis, 1975).

On the other hand, the elongation or shape of the susceptibility ellipsoid does change progressively with increasing cleavage development. Fig-

![Equal-area, lower-hemisphere projections of the principal susceptibility axes for each sample in this study. Bedding planes (north dipping) are shown for the uncleaved samples. Both bedding and cleavage planes (south dipping) are indicated for the cleaved samples. The horizontal scale is the distance from the contact between the Martinsburg Formation and the overlying Shawangunk Formation. Cleavage develops with increasing distance from the contact. The dashed line represents the location in which cleavage is first observed in the field. Cleavage is fully developed 120 m beyond the Shawangunk Formation contact.](image-url)
where $X \geq Y \geq Z$ are the principal strain axes and $k_{\text{max}} \geq k_{\text{int}} \geq k_{\text{min}}$ are the principal susceptibilities. The value of the exponent $\alpha$ is empirical, and is suggested to be dependent upon lithology. Hrouda (1987) listed a value of $\alpha = 0.05$ for slates in general; we have used this value in our apparent-strain calculations. Table 1 lists the magnitudes of the principal susceptibility axes and the calculated apparent-strain values. Following the results in Wintsch and Kvale (1989), who reported that no volume loss occurred with cleavage formation in these rocks, the apparent strain axes $X \geq Y \geq Z$ were calculated using a constant-volume model. These calculations show a clear progression in apparent strain values with developing cleavage; notably a decrease in the magnitude of the $Y$ axis and an increase in the $Z$ axis.

The apparent strain values range from 2.79 : 1.87 : 0.19 for shale (site Om8) to 2.92 : 0.82 : 0.42 for slate (site Om32). At this point we wish to note, however, that we question the geologic relevance of the oblate—prolate boundary ($k = 1$), and continue the trend observed in the uncleaved samples. Fully cleaved samples (125 and 128 m) lie in the prolate field.

4. Discussion

Studies of AMS and rock fabric (e.g. Borradaile, 1988) show that the minimum AMS axis generally lies perpendicular to the dominant planar rock fabric, such as bedding or cleavage (Fig. 4). Our comparison between AMS and rock fabric variations in the Martinsburg Formation, however, does not agree with these observations. Characteristic 'no-cleavage' fabrics from the Martinsburg Formation can be seen in the left half of Fig. 2. The minimum AMS axis is generally 20° away from the pole to bedding. Cleaved samples, on the other hand, display an AMS fabric that appears to be in better agreement with the predicted fabric. Most samples taken from the interval in which the cleavage is developed yield an AMS fabric in which the minimum axis corresponds with the pole to cleavage. There are notable discrepancies, however. The site in which incipient cleavage is initially observed in the field (site Om24) continues to display an AMS fabric with the minimum axis at a high angle to the bedding plane.


TABLE 1
Principal susceptibility axes and calculated apparent strains

<table>
<thead>
<tr>
<th>Site</th>
<th>N</th>
<th>Dist</th>
<th>Susceptibility axes (1 × 10⁻⁶ SI units)</th>
<th>L</th>
<th>F</th>
<th>Apparent strain ratios</th>
<th>Apparent strain axes</th>
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<td></td>
<td></td>
<td></td>
<td>k&lt;sub&gt;max&lt;/sub&gt; k&lt;sub&gt;int&lt;/sub&gt; k&lt;sub&gt;min&lt;/sub&gt;</td>
<td></td>
<td></td>
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<td>Om8</td>
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<td>1.02</td>
<td>1.12</td>
<td>1.51 9.77 2.82</td>
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<td>1.07</td>
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<td>1.27 0.34</td>
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<td>1.04</td>
<td>1.48 2.25 1.70</td>
<td>1.15 0.51</td>
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<td>1.27 1.83 1.44</td>
<td>1.13 0.62</td>
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<td>1.23 0.54</td>
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<td>1.03</td>
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<td>1.00 0.54</td>
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<tr>
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<td>128</td>
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<td>1.07</td>
<td>1.03</td>
<td>3.57 1.95 2.92</td>
<td>0.82 0.42</td>
</tr>
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</table>

a L4–L7 are results from an unpublished pilot study.
b Distance of a sample from the Martinsburg–Shawangunk contact in meters.
c Number of determinations of the susceptibility ellipsoid, each determination is the average of four measurements.
d k<sub>max</sub> > k<sub>int</sub> > k<sub>min</sub> are the principal susceptibility axes.
e Magnetic lineation (k<sub>max</sub>/k<sub>int</sub>).
f Magnetic foliation (k<sub>int</sub>/k<sub>min</sub>).
g Strain ratios are derived from equations in Hrouda (1987), with a = 0.05.
h Strain ellipsoid axes (X ≥ Y ≥ Z) were calculated using a constant-volume model in which X × Y × Z = 1.
i Samples with a sandy lithology.

**Fig. 4.** Typical orientations of the principal susceptibility axes. The minimum axis is expected to be perpendicular to a planar rock fabric, such as bedding in this example. The maximum axis is commonly found at the bedding–cleavage intersection (from Borradaile, 1988).
crystallographic-preferred orientation of chlorite and mica (001) planes, derived from great-circle X-ray scans, expressed as a rake on a reference plane perpendicular to both bedding and cleavage. Bedding and cleavage orientations are also plotted. The horizontal axis indicates the distance from the contact with the Shawangunk Formation.

Both Holeywell and Tullis (1975), and Lee et al. (1986) report a gradual increase in the number of chlorite and mica grains oriented parallel to cleavage over the interval in which cleavage is developed. Orientation of mica grains progresses from parallel-to-bedding to parallel-to-cleavage, with intermediate orientations observed in the interval in which cleavage is developed (Fig. 5b). Orientations of chlorite exhibit two populations: (i) the 'no-cleavage' population, with an (001) orientation at an angle of 20° to bedding as found in the interval from 0 to 110 m, (ii) the 'cleavage' population, with an (001) orientation parallel to the cleavage plane, as found in the interval from 115 to 130 m (Fig. 5b). No chlorite (001) orientation fabrics intermediate to those two patterns are present, in contrast to mica. The lack of intermediate orientations and textural relationships are cited by Holeywell and Tullis (1975) and Lee et al. (1986) as evidence that chlorite reorients entirely via pressure solution and new growth with
the formation of slaty cleavage in the Martinsburg Formation.

Chlorite is a paramagnetic phyllosilicate that, when subjected to a magnetic field, yields a minimum susceptibility axis perpendicular to the (001) plane (Borradaile et al., 1987). Consequently, the intermediate and maximum susceptibility axes lie in the basal plane. For comparison with chlorite orientations, we have plotted the plane containing the intermediate and maximum susceptibility axes as a rake on the reference plane in a manner similar to that for the chlorite basal planes (Fig. 6). Close examination of Fig. 6 shows that both the uncleaved and the cleaved samples exhibit AMS patterns that follow the orientation of chlorite. Like chlorite, AMS orientations are 20° away from the orientation of bedding in uncleaved samples, and are approximately parallel to cleavage in well-cleaved samples. Moreover, no AMS orientations intermediate to these orientations are observed. Additionally, the relative magnitudes of the principal susceptibility axes (Table 1) closely match the susceptibility values of chlorite listed in Borradaile et al. (1987). These combined observations show that AMS is controlled by chlorite in these samples, and provides an explanation for the discrepancy between the orientations of rock fabrics and the AMS axes. The control of AMS by chlorite in these rocks corroborates previous results (e.g. Borradaile et al., 1986) that suggest that paramagnetic matrix minerals may dominate AMS measurements in slates.

The agreement between chlorite and AMS orientations is not perfect, however, as the AMS orientation becomes parallel to cleavage closer to the Martinsburg—Shawangunk contact than does the chlorite orientation. The shift in the dominant chlorite (001) orientation (Fig. 6) occurs 115 m from the Shawangunk Formation contact. On the other hand, the abrupt change in orientation of the AMS fabric occurs at a point ~90 m from the Shawangunk Formation contact, roughly coinciding with the first appearance of cleavage in the field rather than the change in dominant chlorite (001) orientation as measured by texture goniometry. This observation may simply reflect the differing sensitivities of AMS and X-ray methods to changes in bulk crystallographic orientation.

4.2. AMS and strain

Various relationships between strain and AMS have been proposed (e.g. Singh et al., 1975; Hrouda, 1976, 1980; Kligerfield et al., 1977; Rathore, 1979; Rochette and Vialon, 1984). For example, Rathore (1979, 1988) and Hrouda (1987) present results correlating the development of cleavage, strain and AMS in slates. Rathore (1979) related the magnitude of the principal susceptibility axes to March strains in Cambrian slates of North Wales; the equations used previously were derived from this work (Hrouda, 1987). As discussed in the previous section, AMS patterns are controlled by the orientation of chlorite in the Martinsburg Formation samples, and thus, the behavior of chlorite during progressive cleavage development constrains any model relating AMS and strain in the Martinsburg slates (see also Rochette, 1987). The behavior of chlorite in the Martinsburg Formation shale-to-slate transition does not fit the critical assumptions made in Rathore (1979), which call for rigid-body rotation (March-strain model) of the susceptibility-carrier grains as cleavage is formed, and rests upon the assumption that no recrystallization of the susceptibility carriers has occurred. We conclude that if dissolution–neocrystallization of chlorite is characteristic for the formation of cleavage in slates, AMS fabrics record only the degree of pressure solution and new growth. A direct relationship between dissolution–precipitation and strain is not known and, thus, the AMS magnitudes may not represent finite strain.

5. Conclusions

Comparison of AMS and chlorite fabrics in the Martinsburg Formation shale-to-slate transition shows that AMS measures the orientation of chlorite basal planes in these rocks. The abundance of paramagnetic chlorite dominates the susceptibility patterns; other magnetic phases contribute relatively little. Consequently, the ability of AMS to characterize rock fabrics is limited to rock fabrics controlled by, or which control, chlorite orientation. Because the AMS fabric follows the orienta-
tion of chlorite, the behavior of this phyllosilicate during progressive cleavage development determines the apparent strain magnitudes deduced from AMS measurements. In the Martinsburg slates, chlorite undergoes extensive dissolution and neoocrystallization; rotation during progressive cleavage development was absent. Therefore, until models correlating AMS and strain allow for dissolution and precipitation of the susceptibility carriers, the calculated 'strain' values only reflect the degree of pressure solution and new growth and do not necessarily reflect finite strain.

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References


